

Developments in Atmospheric Science, 2

WAVES IN THE ATMOSPHERE

Atmospheric Infrasound and Gravity Waves -
their Generation and Propagation

by

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